

### Year 4 | Autumn Term | Week 10 to 12 – Number: Multiplication & Division



# Overview Small Steps

	-
Multiply by 10	
Multiply by 100	
Divide by 10	
Divide by 100	
Multiply by 1 and 0	
Divide by 1 and itself	
Multiply and divide by 3	R
The 3 times-table	R
Multiply and divide by 6	
6 times table and division facts	
Multiply and divide by 9	
9 times table and division facts	
Multiply and divide by 7	
7 times table and division facts	

### Notes for 2020/21

We have added in the 3 times table steps from year 3 to help support children's understanding of the 6 and 9 times tables and see the links between them.

We feel that it is vital that there is plenty of practice of times table facts. This will help children with their future learning in many areas of mathematics.



### Notes and Guidance

Children need to be able to visualise and understand making a number ten times bigger and that 'ten times bigger' is the same as 'multiply by 10'

The language of 'ten lots of' is vital to use in this step. The understanding of the commutative law is essential because children need to see calculations such as  $10 \times 3$  and  $3 \times 10$  as equal.

### Mathematical Talk

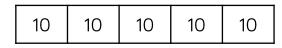
- Can you represent these calculations with concrete objects or a drawing?
- Can you explain what you did to a partner?
- What do you notice when multiplying by 10? Does it always work?

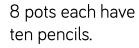
What's the same and what's different about 5 buses with 10 passengers on each and 10 buses with 5 passengers on each?

### Varied Fluency

Tens	Ones	Write the calculation shown by the place
	00000	value counters.
	00000	Each row has tens and ones.
		Each row has a value of
		There are rows.
	00000	The calculation is $\_\_\_ \times \_\_\_ = \_\_$ .
Use p		unters to calculate:
I		
	10 × 3	4 × 10 12 × 10

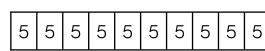
- Match each statement to the correct bar model.
- 5 buses have ten passengers.

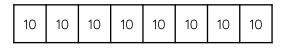




10 chickens lay 5 eggs each.

3







### Reasoning and Problem Solving

### Always, Sometimes, Never

If you write a whole number in a place value grid and multiply it by 10, all the digits move one column to the left.

#### Always.

Discuss the need for a placeholder after the new rightmost digit.

Annie has multiplied a whole number by 10	45 × 10 46 × 10
Her answer is between 440 and 540 What could her original calculation be?	47 × 10 48 × 10 49 × 10
How many possibilities can you find?	50 × 10 51 × 10 52 × 10
	$53 \times 10$ (or the above
	calculations written as $10 \times 45$ etc.).



### Notes and Guidance

Children build on multiplying by 10 and see links between multiplying by 10 and multiplying by 100

Use place value counters and Base 10 to explore what is happening to the value of the digits in the calculation and encourage children to see a rule so they can begin to move away from concrete representations.

Mathematical Talk

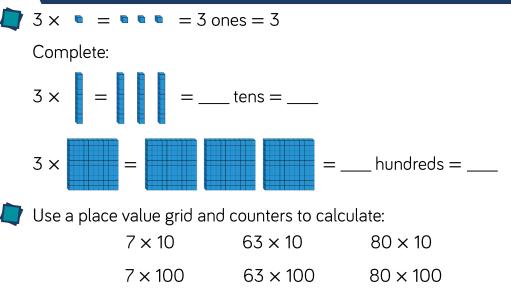
How do the Base 10 help us to show multiplying by 100?

Can you think of a time when you would need to multiply by 100?

Will you produce a greater number if you multiply by 100 rather than 10? Why?

Can you use multiplying by 10 to help you multiply by 100? Explain why.

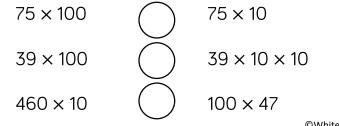
# Varied Fluency



What's the same and what's different comparing multiplying by 10 and 100? Write an explanation of what you notice.

Use <, > or = to make the statements correct.

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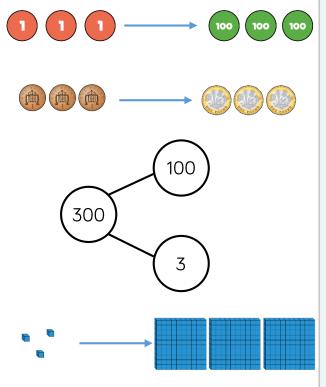


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### Reasoning and Problem Solving

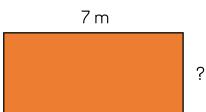
Which representation does **not** show multiplying by 100? Explain your answer.



The part-whole model does not represent multiplying by 100

Part-whole models show addition (the aggregation structure) and subtraction (the partitioning structure), so if the whole is 300 and there are two parts, the parts added together should total 300 (e.g. 100 and 200, or 297 and 3). If the parts are 100 and 3, the whole should be 103.

To show multiplying 3 by 100 as a partwhole model, there would need to be 100 parts each with 3 in. The perimeter of the rectangle is 26 m. Find the length of the missing side. Give your answer in cm.



The missing side length is 6 m so in cm it will be:

 $6 \times 100 = 600$ 

The missing length is 600 cm.



### Notes and Guidance

- Exploring questions with whole number answers only, children divide by 10
- They should use concrete manipulatives and place value charts to see the link between dividing by 10 and the position of the digits before and after the calculation.
- Using concrete resources, children should begin to understand the relationship between multiplying and dividing by 10 as the inverse of the other.

### Mathematical Talk

- What has happened to the value of the digits?
- Can you represent the calculation using manipulatives? Why do we need to exchange tens for ones?
- When dividing using a place value chart, in which direction do the digits move?

### Varied Fluency

Use place value counters to show the steps to divide 30 by 10

10 10 10

Can you use the same steps to divide a 3-digit number like 210 by 10?

100 100 10

Use Base 10 to divide 140 by 10 Explain what you have done.

- Ten friends empty a money box. They share the money equally between them. How much would they have each if the box contained:
  - 20 £1 coins?
  - £120
  - £24?

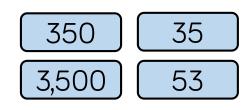
After emptying the box and sharing the contents equally, each friend has 90 p.

How much money was in the box?



### **Reasoning and Problem Solving**

Four children are in a race. The numbers on their vests are:



Use the clues to match each vest number to a child.

- Jack's number is ten times smaller than Mo's.
- Alex's number is not ten times smaller than Jack's or Dora's or Mo's.
- Dora's number is ten times smaller than Jack's.

Alex - 53 Jack - 350 Dora - 35 Mo - 3,500 While in Wonderland, Alice drank a potion and everything shrank. All the items around her became ten times smaller! Are these measurements correct?

ltem	Original measurement	After shrinking
Height of a door	220 cm	2,200 cm
Her height	160 cm	16 cm
Length of a book	340 mm	43 mm
Height of a mug	220 mm	?

Can you fill in the missing measurement?

Can you explain what Alice did wrong?

Write a calculation to help you explain each item.

Height of a door Incorrect – Alice has multiplied by 10.

<u>Her height</u> Correct

Length of a book Incorrect – Alice has swapped the order of the digits. When dividing by 10 the order of the digits never changes.

Height of a mug 22 mm.



### Notes and Guidance

Children divide by 100 with whole number answers.

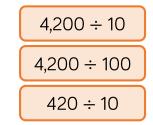
Money and measure is a good real-life context for this, as coins can be used for the concrete stage.

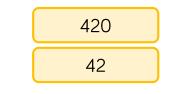
### Varied Fluency

Is it possible for £1 to be shared equally between 100 people? How does this picture explain it? Can £2 be shared equally between 100 people? How much would each person receive?



Match the calculation with the correct answer.





Use <, > or = to make each statement correct.

$$3,600 \div 10$$
 $3,600 \div 100$  $2,700 \div 100$  $270 \div 10$  $4,200 \div 100$  $430 \div 10$ 

### Mathematical Talk

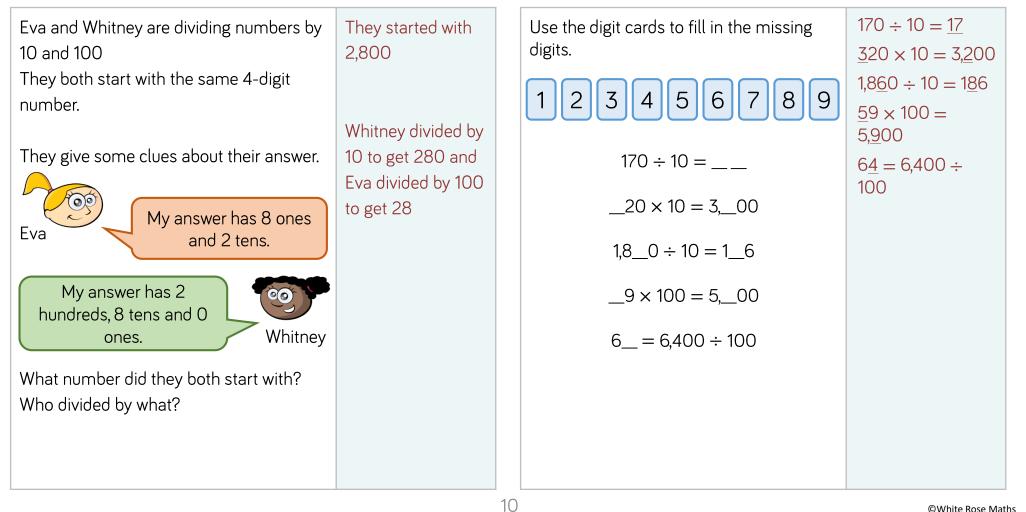
How can you use dividing by 10 to help you divide by 100?

How are multiplying and dividing by 100 related?

Write a multiplication and division fact family using 100 as one of the numbers.



### **Reasoning and Problem Solving**



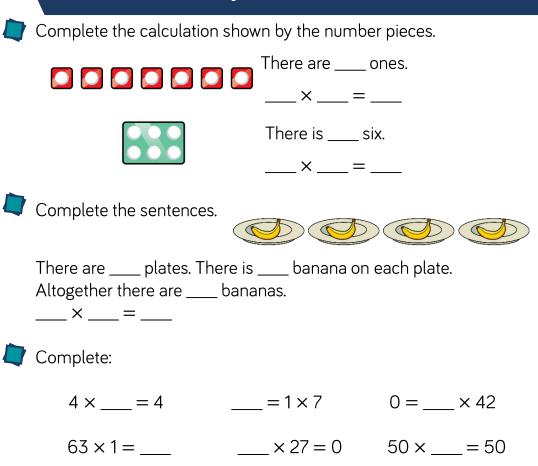


### Multiply by 1 and 0 Notes and Guidance Children explore the result of multiplying by 1, using concrete equipment.

Linked to this, they look at multiplying by 0 and use concrete equipment and pictorial representations of multiplying by 0

### Varied Fluency

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### Mathematical Talk

Use number pieces to show me  $9 \times 1, 3 \times 1, 5 \times 1$ 

What do you notice?

What does 0 mean?

What does multiplying by 1 mean?

What's the same and what's different about multiplying by 1 and multiplying by 0?



### Multiply by 1 and 0

### **Reasoning and Problem Solving**

Which answer could be the odd one out? What makes it the odd one out?

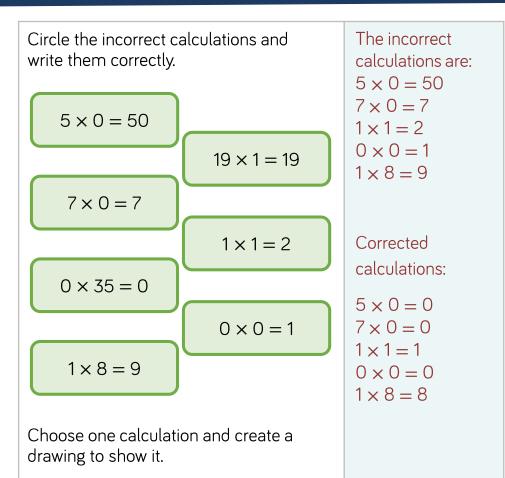
- 3 + 0 = \_\_\_\_ 3 - 0 =
- 3 × 0 = \_\_\_\_

Explain why the answer is different.

 $3 \times 0 = 0$  is the odd one out because it is the only one with 0 as an answer. The addition and

subtraction calculations have an answer of 3 because they started with that amount and added or subtracted 0 (nothing).

 $3 \times 0$  means '3 lots of nothing', so the total is zero.





### Notes and Guidance

Children learn what happens to a number when you divide it by 1 or by itself. Using concrete and pictorial representations, children demonstrate how both the sharing and grouping structures of division can be used to divide a number by 1 or itself. Use stem sentence to encourage children to see this e.g. 5 grouped into 5s equals  $1 (5 \div 5 = 1)$ 5 grouped into 1s equals  $5 (5 \div 1 = 5)$ 

### Mathematical Talk

What does sharing mean? Give an example.

- What does grouping mean? Give an example.
- Can you write a worded question where you need to group?
- Can you write a worded question where you need to share?

### Varied Fluency

Vuse counters and hands to complete.

- 4 counters shared between 4 hands
- 4 counters shared between 1 hand
- 9 counters grouped in 1s
- 9 counters **grouped** in 9s

÷_	=	
÷.	=	
÷_	=	
÷	=	

Choose the correct bar model to help you answer this question. Annie has £4 in total. She gives away £4 at a time to her friends. How many friends receive £4?

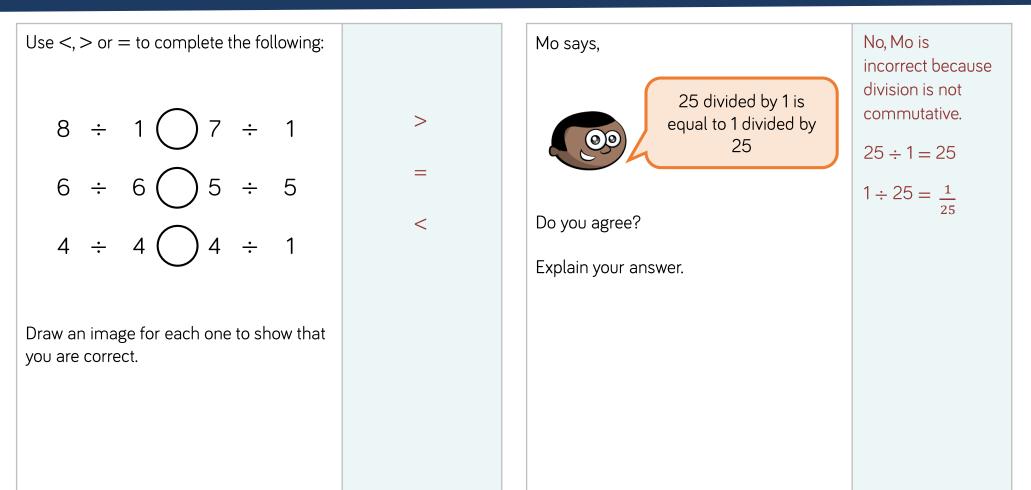
	£4			£4
£1	£1	£1	£1	£4



- Draw a bar model for each question to help you work out the answer.
- Tommy baked 7 cookies and shared them equally between his 7 friends. How many cookies did each friend receive?
- There are 5 sweets. Children line up and take 5 sweets at a time. How many children have 5 sweets?



### **Reasoning and Problem Solving**





### Notes and Guidance

Children draw on their knowledge of counting in threes in order to start to multiply by 3

They use their knowledge of equal groups to use concrete and pictorial methods to solve questions and problems involving multiplying by 3

### Mathematical Talk

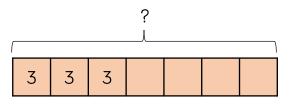
How many equal groups do we have?

- How many are in each group?
- How many do we have altogether?
- Can you write a number sentence to show this?
- Can you represent the problem in a picture?
- Can you use concrete apparatus to solve the problem?
- How many lots of 3 do we have?
- How many groups of 3 do we have?

### Varied Fluency

There are five towers with 3 cubes in each tower. How many cubes are there altogether?

#### There are 7 tricycles in a playground. How many wheels are there altogether? Complete the bar model to find the answer.



There are 3 tables with 6 children on each table. How many children are there altogether?

\_\_\_\_ lots of \_\_\_\_ = \_\_\_\_

× =



### Reasoning and Problem Solving

There are 8 children.		
Each child has 3 sweets.		
How many sweets altogether?		

Use concrete or pictorial representations to show this problem.

Write another repeated addition and multiplication problem and ask a friend to represent it. There are 24 sweets altogether. Children may use items such as counters or cubes. They could draw a bar model for a

pictorial

representation.

se • 5 × 3 + 6

• 5 × 3 + 3

If  $5 \times 3 = 15$ , which number sentences

would find the answer to  $6 \times 3$ ?

- 15 + 3
- 15 + 6
- 3 × 6

Explain how you know.

 $5 \times 3 + 3$ because one more lot of 3 will find the answer.

15 + 3 because adding one more lot of 3 to the answer to 5 lots will give me 6 lots.

 $3 \times 6$  because  $3 \times 6 = 6 \times 3$ (because multiplication is commutative).





### Notes and Guidance

Children explore dividing by 3 through sharing into three equal groups and grouping in threes.

They use concrete and pictorial representations and use their knowledge of the inverse to check their answers.

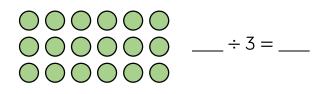
### Mathematical Talk

Can you put the counters into groups of three?

- Can you share the number into three groups?
- What is the difference between sharing and grouping?

### Varied Fluency

Circle the counters in groups of 3 and complete the division.

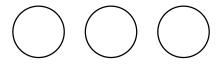


Circle the counters in 3 equal groups and complete the division.

What's different about the ways you have circled the counters?

There are 12 pieces of fruit. They are shared equally between 3 howls. How many pieces of fruit are in each how!?

bowls. How many pieces of fruit are in each bowl? Use cubes/counters to represent fruit and share between 3 circles.





Bobbles come in packs of 3 If there are 21 bobbles altogether, how many packs are there?



### Reasoning and Problem Solving

Share 33 cubes between 3 groups.

#### Complete:

There are 3 groups with \_\_\_\_\_ cubes in each group.  $33 \div 3 = \____$ 

Put 33 cubes into groups of 3

#### Complete:

There are \_\_\_\_\_ groups with 3 cubes in each group.  $33 \div 3 =$ \_\_\_\_

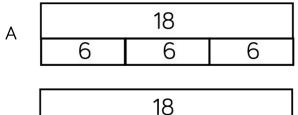
What is the same about these two divisions? What is different?

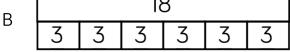
The number sentences are both the same. The numbers in each number sentence mean different things. In the first question, the '3' means the number of groups the cubes are shared into because the cubes are being shared. In the second question, the '3' means the size of each group.

#### Jack has 18 seeds.

He plants 3 seeds in each pot.

Which bar model matches the problem?





Explain your choice.

Bar model B matches the problem because Jack plants 3 seeds in each pot, therefore he will have 6 groups (pots), each with 3 seeds.



### The 3 Times Table

### Notes and Guidance

Children draw together their knowledge of multiplying and dividing by three in order to become more fluent in the three times table.

Children apply their knowledge to different contexts.

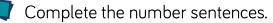
Mathematical Talk

Can you use concrete or pictorial representations to help you?

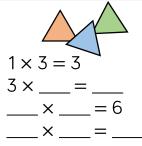
What other facts can you link to this one?

What other times table will help us with this question?

### Varied Fluency



1 triangle has 3 sides	
3 triangles have	sides in total.
triangles have 6	sides in total.
5 triangles have	sides in total.



Tick the number sentences that the image shows.



1 × 3 =	×3=30
2 × = 6	8 × = 24
= 3 × 3	6 × 3 =
9 × 3 =	$21 = \times 3$



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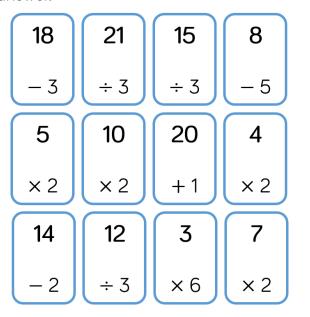
### The 3 Times Table

### Reasoning and Problem Solving

Sort the cards below so they follow round Order: in a loop.

Start at 18 - 3

Calculate the answer to this calculation. The next card needs to be begin with this answer.



multiples of three. On the 15th beat, I
On the 15th beat, I
will be clicking because 15 is a multiple of 3
On the 20th beat, I will be clapping
because 20 is not a multiple of 3



# Multiply and Divide by 6

### Notes and Guidance

Children draw on their knowledge of times tables facts in order to multiply and divide by 6

They use their knowledge of equal groups in using concrete and pictorial methods to solve multiplication and division problems.

Mathematical Talk

How many equal groups do we have? How many are in each group? How many do we have altogether?

Can you write a number sentence to show this?

Can you represent the problem in a picture?

What does each number in the calculation represent?

### Varied Fluency

Complete the sentences.



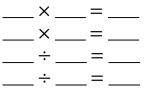
There are \_\_\_\_ lots of \_\_\_\_ eggs. There are <u>eggs</u> in total. × =

First there were \_\_\_\_\_ eggs. Then they were shared into \_\_\_\_\_ boxes. Now there are <u>eggs</u> in each box.

\_\_\_÷\_\_\_=\_\_\_



Complete the fact family.



There are 9 baskets.

Each basket has 6 apples in.

How many apples are there in total?

Write a multiplication sentence to describe this word problem.



### Multiply and Divide by 6

### **Reasoning and Problem Solving**

### Always, Sometimes, Never

When you multiply any whole number by 6 it will always be an even number.

Explain your answer.

Always, because 6 itself is even and odd × even and even × even will always give an even product.

Teddy says,Teddy is not  
correct because 12  
$$\div 6 = 2 \text{ not } 72$$
If  
 $6 \times 12 = 72$   
then  
 $12 \div 6 = 72$ Image: Second secon



### 6 Times Table & Division Facts

### Notes and Guidance

- Children use known table facts to become fluent in the six times table.
- For example, applying knowledge of the 3 times table by understanding that each multiple of 6 is double the equivalent multiple of 3
- Children should also be able to apply this knowledge to multiplying and dividing by 10 and 100 (for example, knowing that  $30 \times 6 = 180$  because they know that  $3 \times 6 = 18$ ).

### Mathematical Talk

What do you notice about the 3 times table and the 6 times table?

Can you use  $3 \times \_$  to work out  $6 \times \_$ ?

Can you use  $7 \times 5$  to work out  $7 \times 6$ ?

Which known fact did you use?

### Varied Fluency

Complete the number sentences.

1 × 3 =	1 × = 6
2 × = 6	2 × 6 =
3 × 3 =	3 × 6 =

m 7 What do you notice about the 5 times table and the 6 times table?

<b>5 times table:</b> 5	10	15	20	25	30
6 times table: 6	12	18	24	30	36

Use your knowledge of the 6 times table to complete the missing values?

$$6 \times 2 = \_ \\ x & 6 = 12 \\ x & 20 = 120 \\ 6 \times \_ = 1,200 \\ 200 \times 6 = \_ \\ 10 \times \_ \times 6 = 120 \\ 10 \times \_ \times 6 = 120$$



### 6 Times Table and Division Facts

### Reasoning and Problem Solving

I am thinking of 2 numbers where the sum of the numbers is 15 and the product is 54 What are my numbers? Think of your own problem for a friend to solve?	6 and 9 because $9 \times 6 = 54$ $6 \times 9 = 54$ 6 + 9 = 15 9 + 6 = 15	Choose the correct number or symbol from the cloud to fill in the boxes. $10^{0} \times 600$ $= 10^{-10} \div 6$	600 ÷ 100 = 6 60 = 600 ÷ 10
Always, Sometimes, Never If a number is a multiple of 3 it is also a multiple of 6 Explain why you think this.	Sometimes. Every even multiple of 3 is a multiple of 6, but the odd multiples of 3 are not multiples of 6	÷=6 60 = 60010	



### Multiply and Divide by 9

### Notes and Guidance

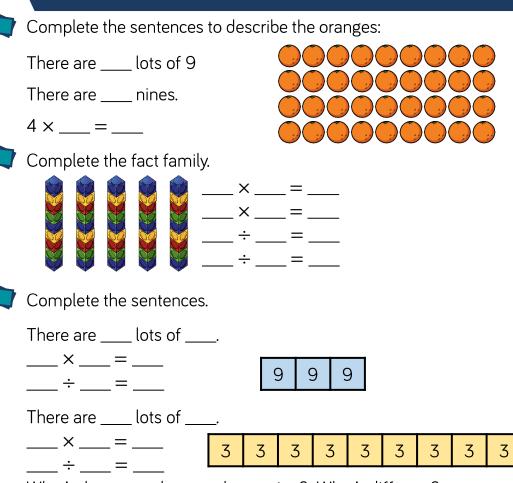
Children use their previous knowledge of multiplying and dividing to become fluent in the 9 times table.

They apply their knowledge in different contexts.

### Mathematical Talk

- Can you use concrete or pictorial representations to help you answer the questions?
- What other facts can you link to this fact?
- What other times tables will help you with this times table?
- What does each number in the calculation represent?
- How many lots of 9 do we have?
- How many groups of 9 do we have?

### Varied Fluency



What's the same about each question? What's different?



### Multiply and Divide by 9

### **Reasoning and Problem Solving**

True or False?	$6 \times 9 = 9 \times 3 \times 2$	Amir and Whitney both receive some sweets.	They both have 54 sweets, arranged
$6 \times 9 = 9 \times 3 \times 2$ $9 \times 6 = 3 \times 9 + 9$	is true because $6 \times 9 = 54$ and		in two different arrays.
$9 \times 0 = 5 \times 9 + 9$ Explain your answer.	$9 \times 3 = 27$ $27 \times 2 = 54$	I have more sweets because I have more	
	$9 \times 6 = 3 \times 9 +$ 9 is false because $6 \times 9 = 54$ and $3 \times 9 = 27$	Amir rows. I have more sweets because I have more in each row. Whitney	
	27 + 9 = 36	Who has more sweets? Explain your	
		reasoning.	



### 9 Times Table & Division Facts

### Notes and Guidance

- Children use known times table facts to become fluent in the 9 times table.
- For example, knowing that each multiple of 9 is one less than the equivalent multiple of 10, and using that knowledge to derive related facts.
- Children should also be able to apply the knowledge of the 9 times table when multiplying and dividing by 10 and 100

### Mathematical Talk

- How did you work out the missing numbers?
- What do you notice about the multiples of 9?
- What do you notice about the 9 times table and the 10 times table?

### Varied Fluency

									i .
	Wha	t are the	missing	numb	ers f	rom the	e 9 times	stable?	
			9	18		27		45	
			54		_	72	81	90	
	Circl	e the m	ultiples o	f 9.					
		54	108	18	24	9	67	72	37
	Use y value	•	owledge (	of the S	9 tim	ies table	e to com	plete the	e missing
		1×9=			_×´	1 = 9	1	×9×_	= 90
		×9	= 90	900	) = 1	00 × _	9	$\times 1 \times 10^{-10}$	) =
	9:	×=	= 900	4 ×	9 =		9:	×1×	_= 900
7	Wha	t do you	notice a	bout th	ne 9 <sup>.</sup>	times ta	able and	the 10 ti	mes table?

<b>9</b> times table: 9	18	27	36	45	54
10 times table: 10	) 20	30	40	50	60



### **9** Times Table and Division Facts

### Reasoning and Problem Solving

Can you complete the calculations using some of the symbols or numbers in the box? $\begin{array}{ccc} \div & 9 & 100\\ 10 & 900 & = \end{array}$	900 ÷ 100 = 9 90 = 900 ÷ 10	I am thinking of two numbers. The sum of the numbers in 17. The product of the numbers is 72. What are my secret numbers? Can you choose your own two secret numbers from the 9 times table and create clues for your partner?	8 and 9 because $8 \times 9 = 72 \text{ or}$ $9 \times 8 = 72$ and 8 + 9 = 17  or 9 + 8 = 17
÷=9 90=90010		Always, Sometimes, Never All multiples of 9 have digits that have a sum of 9.	Always.



# Multiply and Divide by 7

### **Notes and Guidance**

- Children use their knowledge of multiplication and division to multiply by 7
- They count in 7s, and use their knowledge of equal groups supported by use of concrete and pictorial methods to solve multiplication calculations and problems.
- They explore commutativity and also understand that multiplication and division are inverse operations.

### Mathematical Talk

How many do we have altogether?

What do you notice?

- Can you work out the answers by partitioning 7 into 4 and 3?
- Which multiples of 7 do you already know from your other tables?

### Varied Fluency

- Use a number stick to support counting in sevens. What do you notice?
- Write down the first five multiples of 7

Rosie uses number pieces to represent seven times four. She does it in two ways.

4 sevens	7 fours
4 lots of 7	7 lots of 4
4 × 7	7×4



Use Rosie's method to represent seven times six in two ways.

Seven children share 56 stickers. How many stickers will they get each?

Use a bar model to solve the problem.

One apple costs 7 pence. How much would 5 apples cost? Use a bar model to solve the problem.



### Multiply and Divide by 7

### **Reasoning and Problem Solving**

Mrs White's class are selling tickets at £2 each for the school play. The class can sell one ticket for each chair in the hall.	Number of tickets (chairs): $7 \times 9 = 63$	What do you notice about the pattern when counting in 7s from 0? Does this continue beyond 7 times 12? Can you explain why?	Odd, even patter because odd + odd = even. Then even + odd =
There are 7 rows of chairs in the hall. Each row contains 9 chairs. How much money will they make?	63 × £2 = £126	In which other times tables will you see the same pattern?	odd, and this will continue throughout the whole times table.
			The same patter will occur in all other odd multiplication tables (e.g. 1, 3, 5, 9).



### 7 Times Table & Division Facts

### Notes and Guidance

Children apply the facts from the 7 times table (and other previously learned tables) to solve calculations with larger numbers.

They need to spend some time exploring links between multiplication tables and investigating how this can help with mental strategies for calculation.

e.g.  $7 \times 7 = 49, 5 \times 7 = 35$  and  $2 \times 7 = 14$ 

### Mathematical Talk

If you know the answer to three times seven, how does it help you?

What's the same and what's different about the number facts?

How does your 7 times table help you work out the answers?

### Varied Fluency

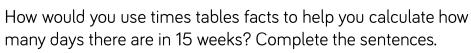


3 × 7 =
30 × 7 =
$300 \times 7 =$

Use your knowledge of the 7 times table to calculate.

 $80 \times 7 =$  $= 60 \times 7$ 

 $70 \times 7 = 7 \times 500 =$ 



There are <u>days</u> in one week.

 $\_$  × 10 =  $\_$ There are \_\_\_\_ days in 10 weeks.

× 5 = There are \_\_\_\_ days in 5 weeks.

\_\_+\_\_=\_\_\_ There are \_\_\_\_\_ days in 15 weeks. 31



### 7 Times Table & Division Facts

### Reasoning and Problem Solving

### True or False?

 $7 \times 6 = 7 \times 3 \times 2$ 

 $7 \times 6 = 7 \times 7 + 8$ 

Explain your answer to a friend. Prove using a drawing.

Т	rue.	

False, because 7 × 6 = 42 whereas 7 × 7 = 49 then 49 + 8 = 57

Children could draw a bar model or bundles of straws. Children were arranged into rows of seven. There were 5 girls and 2 boys in each row.

TITI

Use your times table knowledge to show how many girls would be in 10 rows and in 100 rows.

Show as many number sentences using multiplication and division as you can which are linked to this picture.

How many children in total are there in 200 rows? How many girls? How many boys?

<u>10 rows</u>

 $5 \times 10 = 50$  girls

<u>100 rows</u>

 $5 \times 100 = 500$  girls

#### 200 rows

Children in total: 7 × 200 = 1,400

Girls: 5 × 200 = 1,000

Boys: 2 × 200 = 400